



**Università degli Studi di Padova**  
**Laurea Magistrale in Ingegneria Elettronica**

# Analysis and implementation of a cold start oscillator for ultra low voltage energy harvesting applications

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# Motivating Example: Wireless Sensor Networks

Function of a WSN:

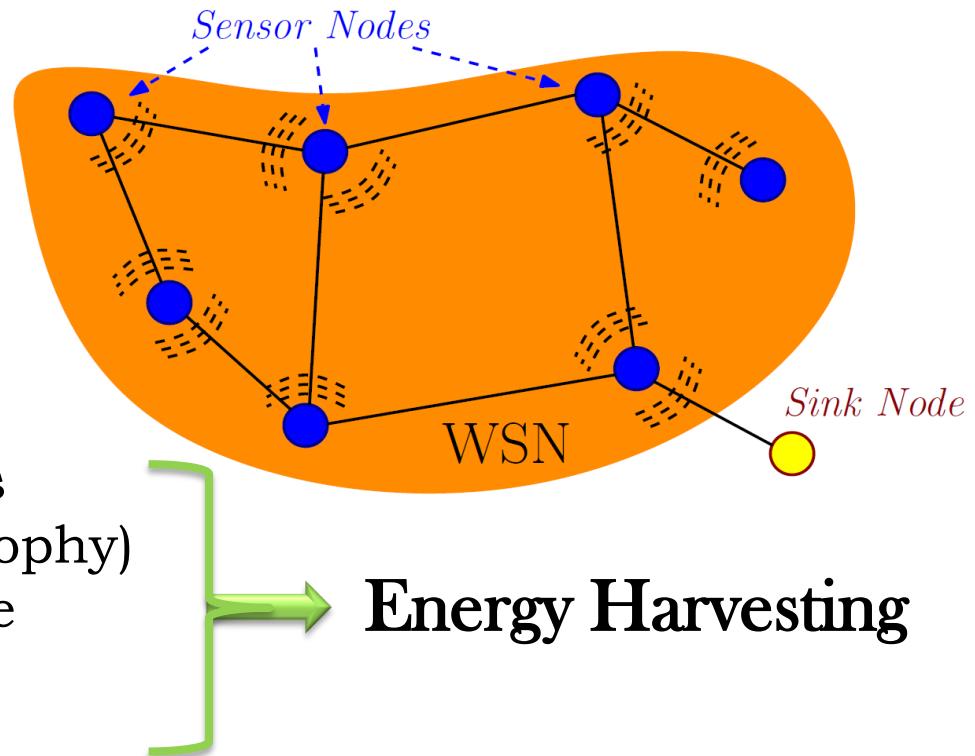
- Sense and sample: temperature, pressure, humidity, etc...
- Route sensed information to a central unit or *sink node*.

Large-scale WSN:

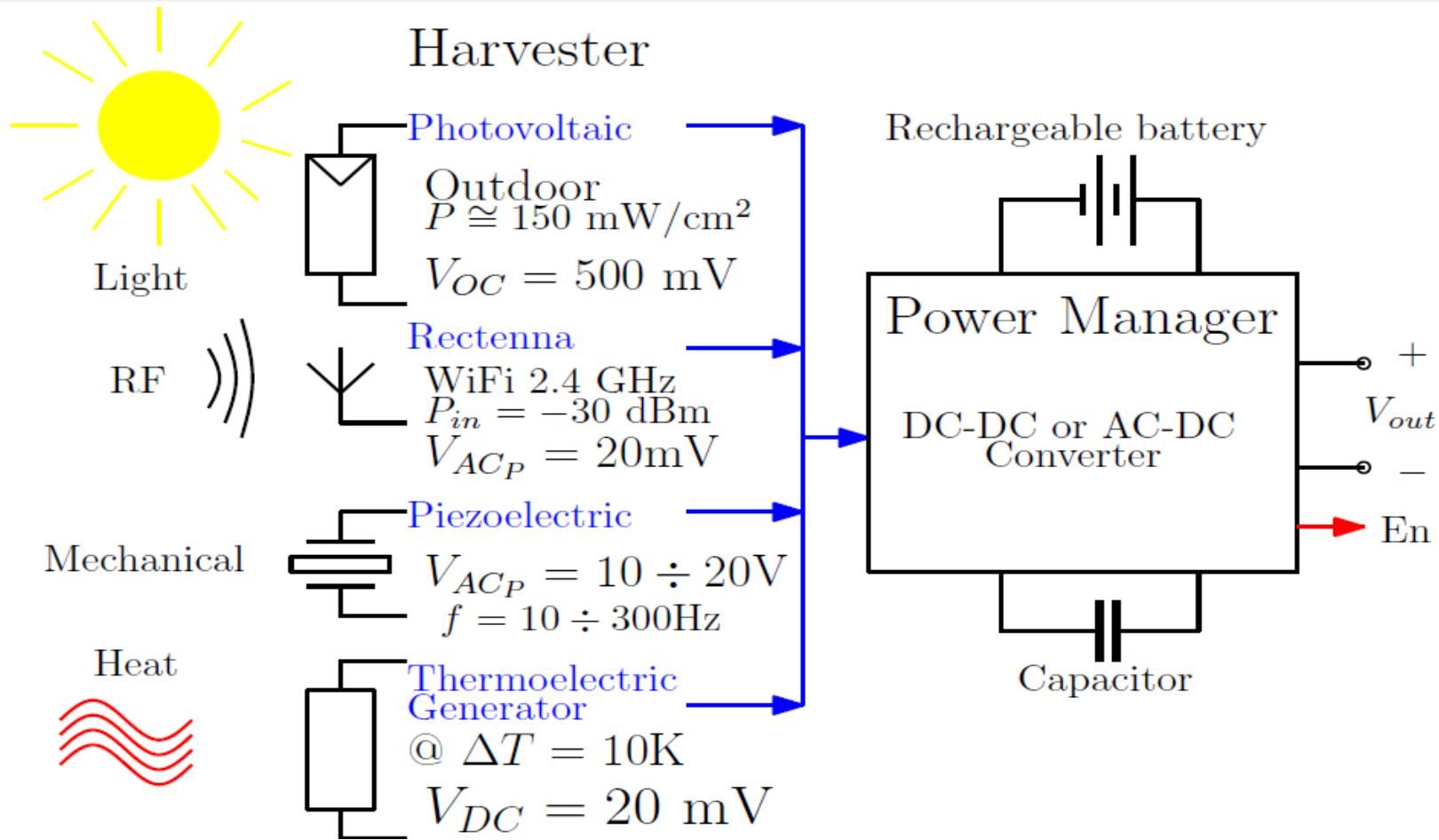
tens to hundreds of nodes

Practical deployment of  
large-scale WSN's implies:

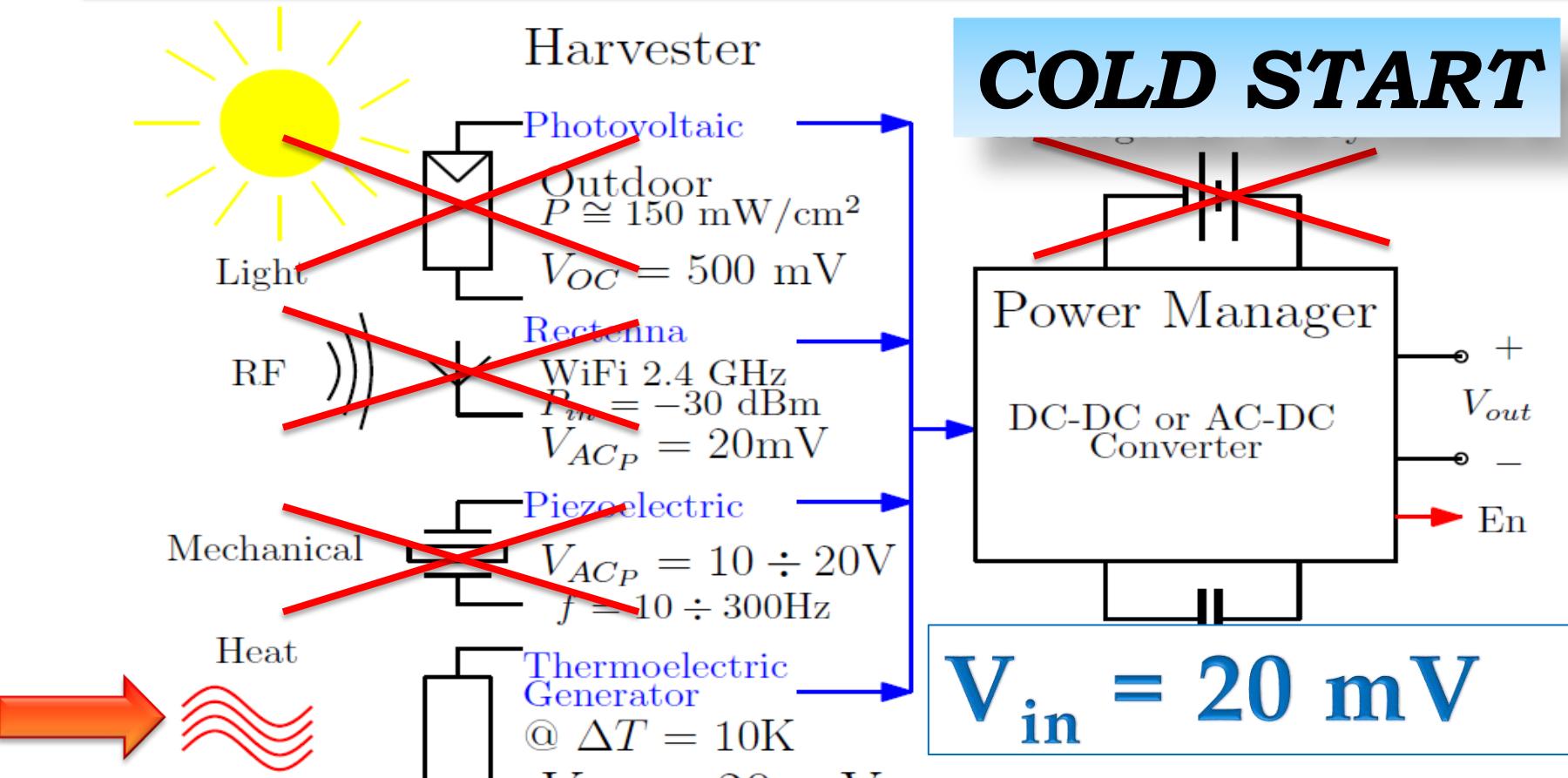
- Zero-maintenance nodes  
("Fit and forget" philosophy)
- Prolonged sensor lifetime  
(e.g. > 2 years)
- Low \$/Wh



# Energy Harvesting System



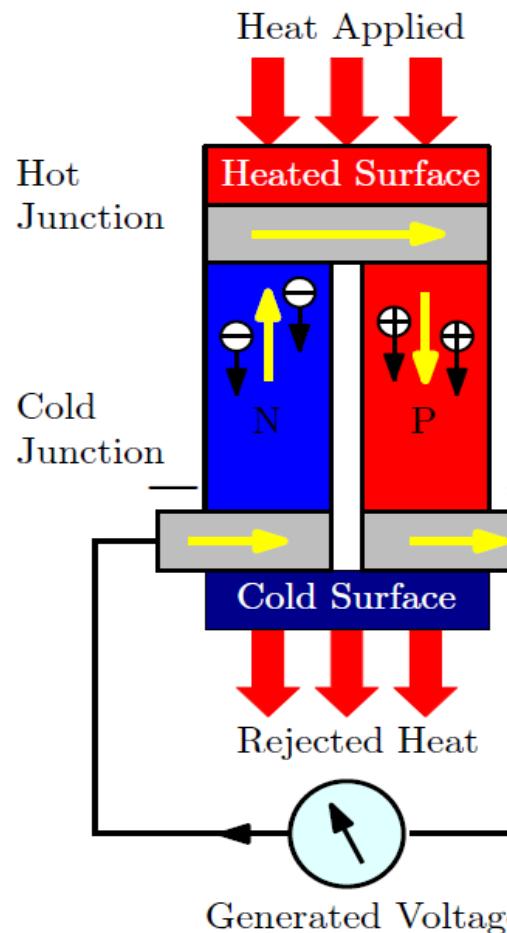
# Energy Harvesting System



**Thesis goal: to develop a cold start circuit for the thermoelectric generator.**

# Thermoelectric Generation

Seebeck Effect

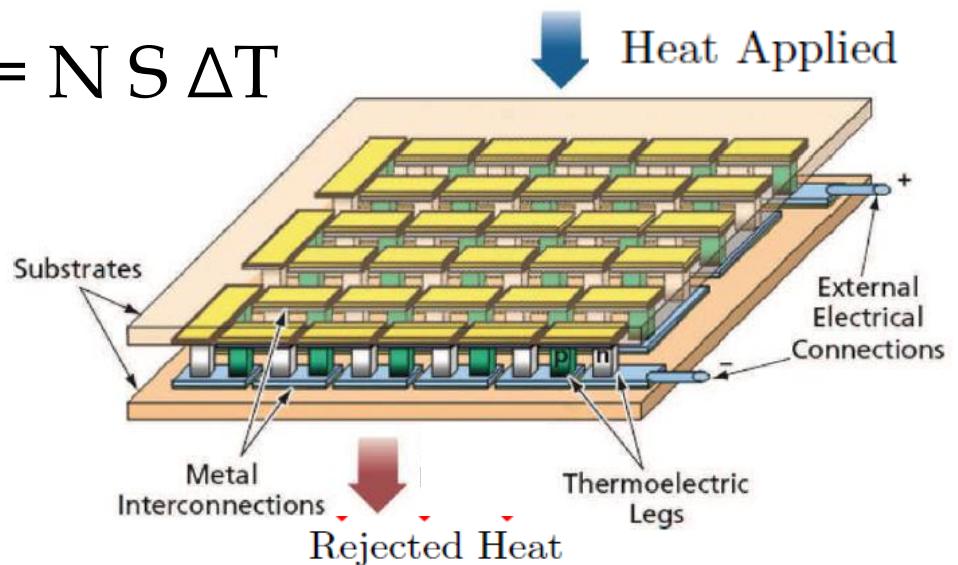


$pn$  junction -  $\text{Bi}_2\text{Te}_3$

$\sim 0.2 \text{ mV/K}$  per cell

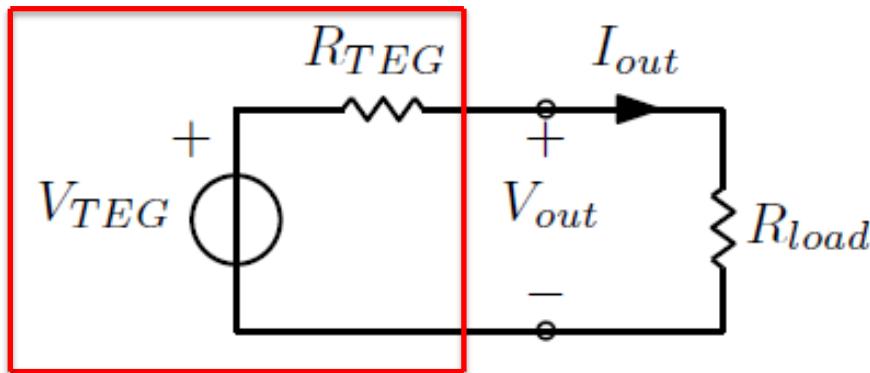
$\sim 20 \text{ mV}$  with 10 cells at  $\Delta T = 10 \text{ K}$

$$V_{\text{out}} = N S \Delta T$$



# Thermoelectric Generation

Thévenin equivalent circuit:

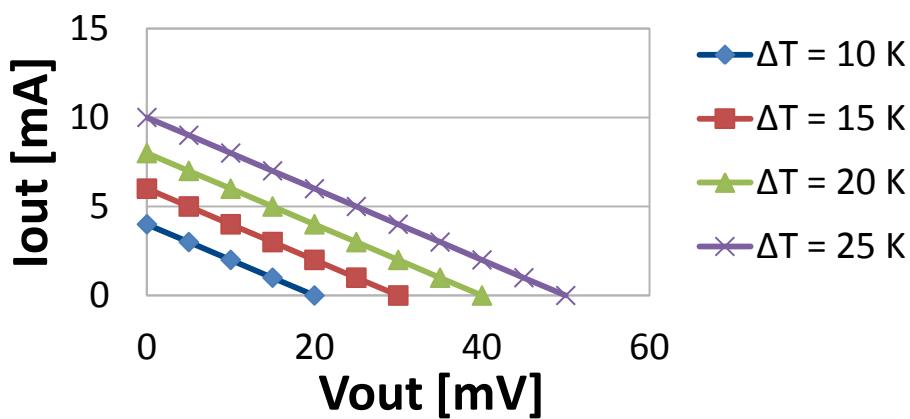


Typ.

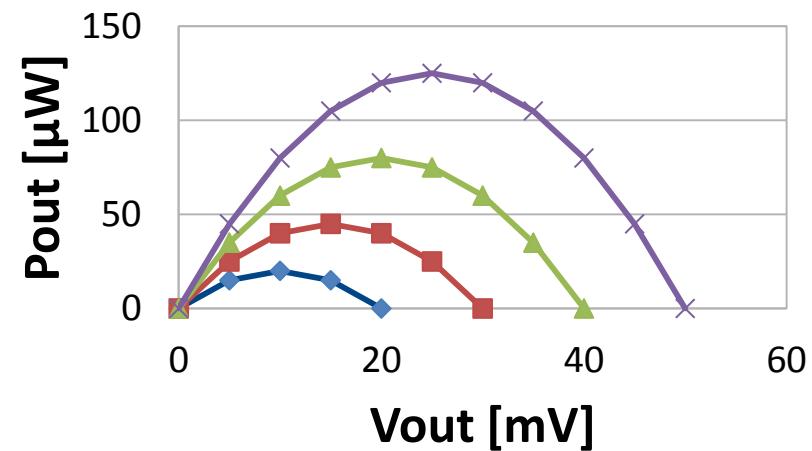
$$R_{TEG} = 2.5 \Omega$$

$$V_{TEG} = \sim 2 \text{ mV/K}$$

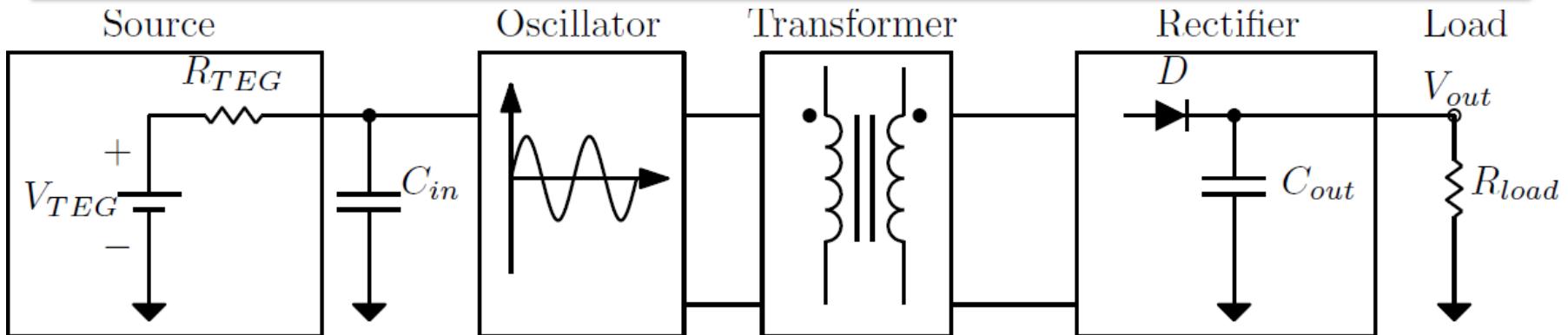
$I_{out}$  vs.  $V_{out}$  @ Delta T



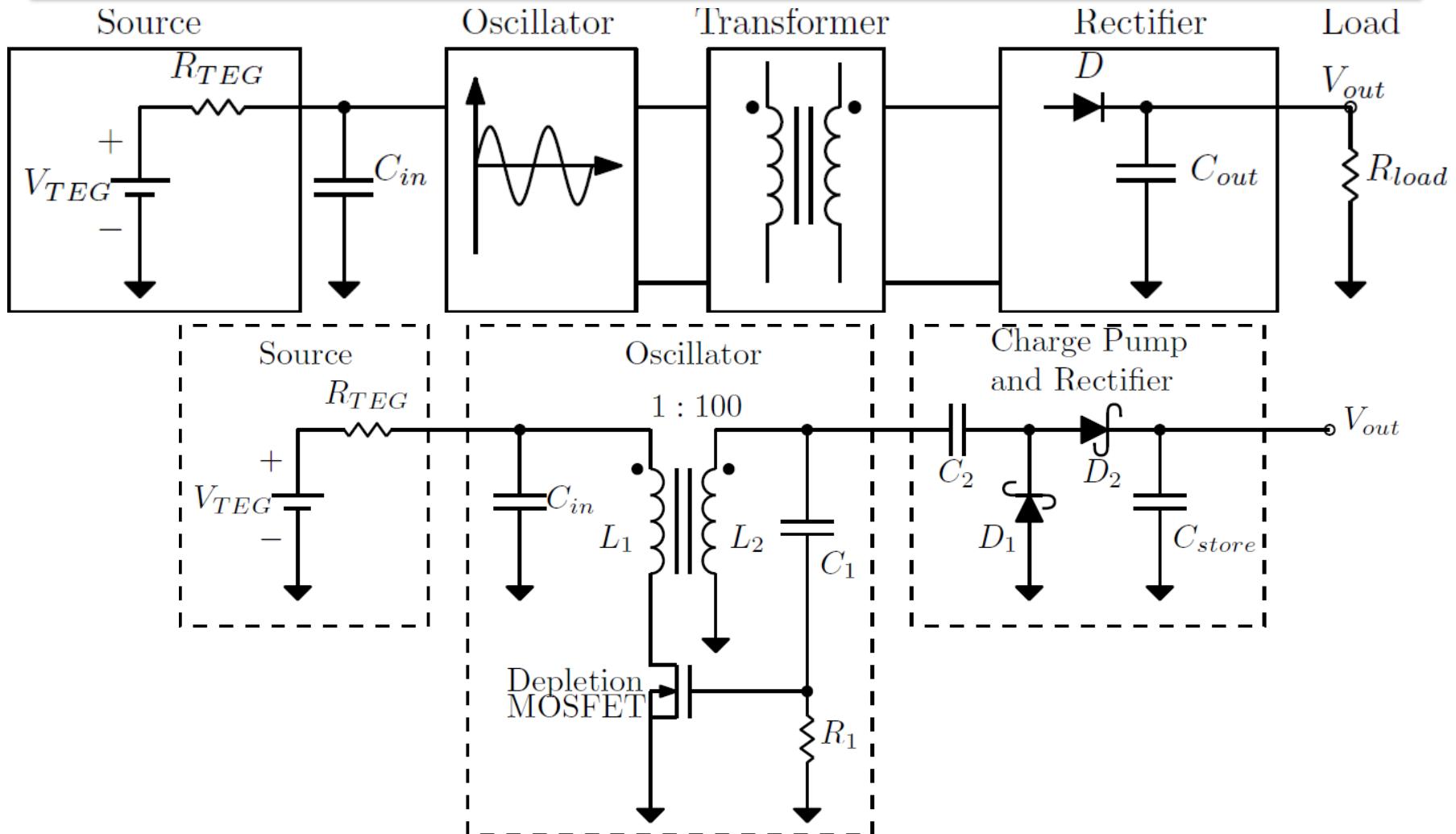
$P_{out}$  vs.  $V_{out}$  @  $\Delta T$



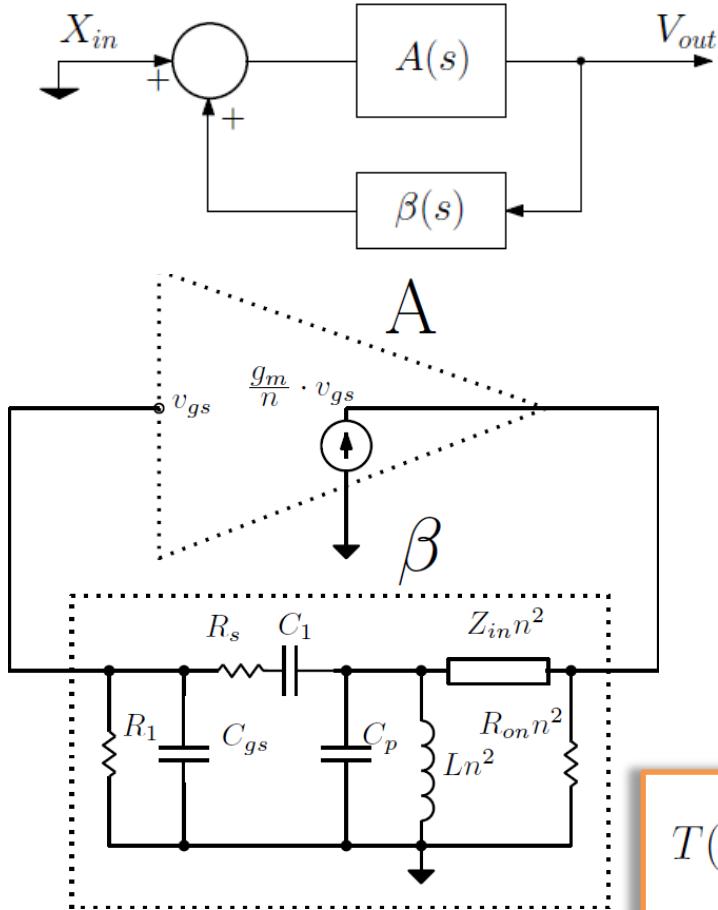
# Cold Start Oscillator for Ultra Low-Voltage Sources



# Cold Start Oscillator for Ultra Low-Voltage Sources



# Oscillator Analysis and Start-Up Condition

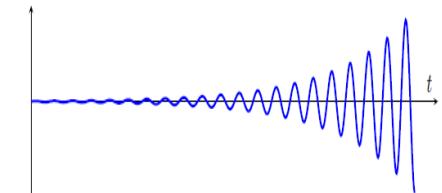


$$1 - A(s)\beta(s) = 0 \quad \Rightarrow \quad 1 - T(s) = 0$$

**Start-up condition**

$$|T(j\omega_0)| > 1$$

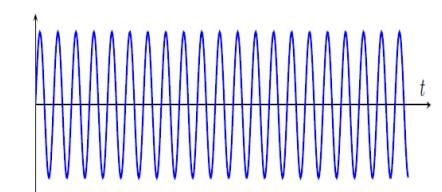
$$\angle T(j\omega_0) = 0^\circ$$



**Barkhausen criterion**

$$|T(j\omega_0)| = 1$$

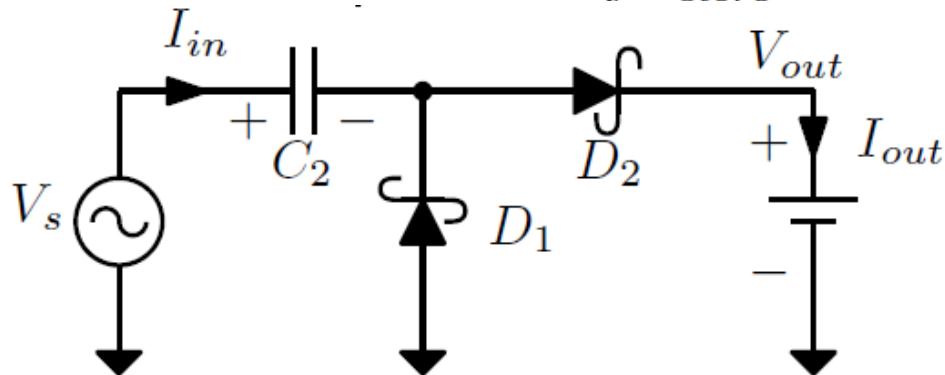
$$\angle T(j\omega_0) = 0^\circ$$



$$T(j\omega_0) = \frac{g_m}{n} \frac{R_{on} \cdot n^2 \cdot (R_1 || R_{in})}{R_{on} \cdot n^2 + [(R_1 || R_{in}) + (R_s + R_p \cdot n^2)]}$$

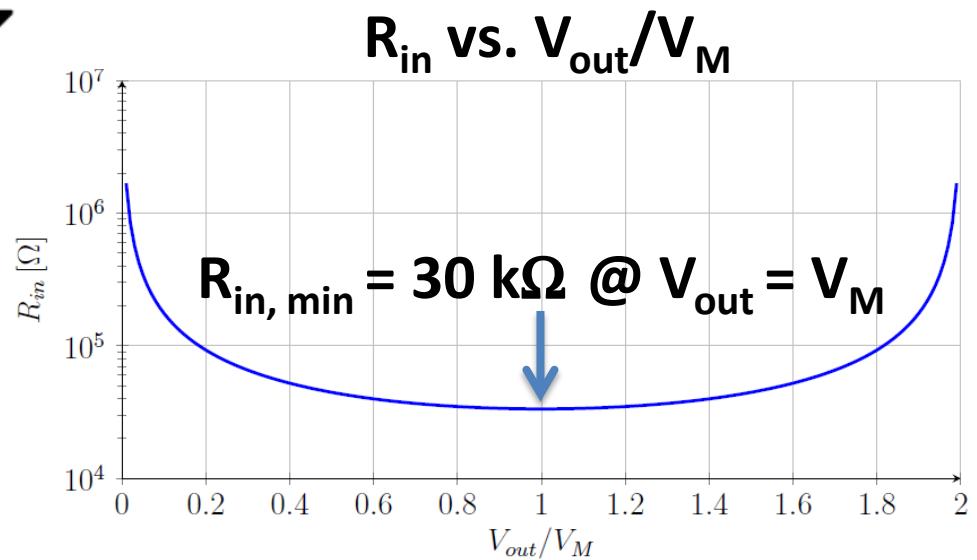
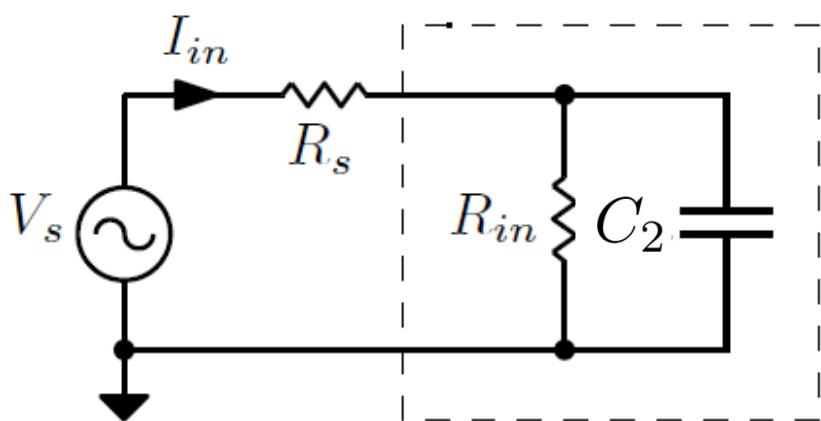
# Analysis of the Rectifying Cell

$$V_{out} = 2V_{M_{in}} - \frac{I}{2fC_{store}}$$

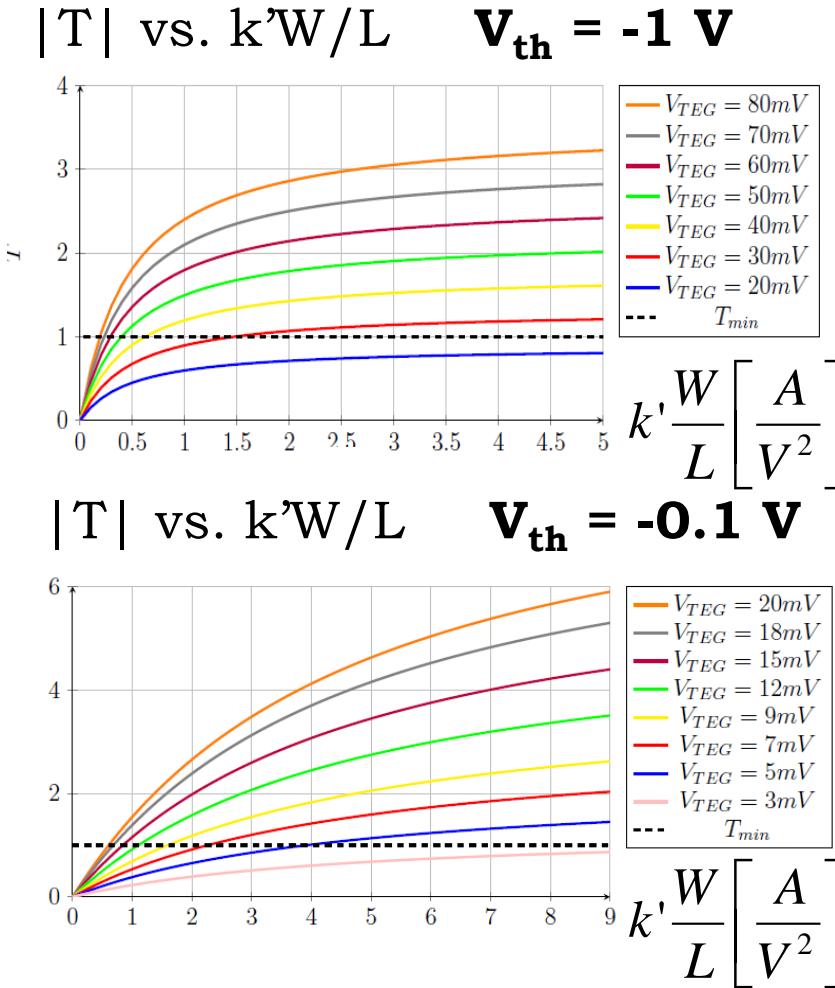
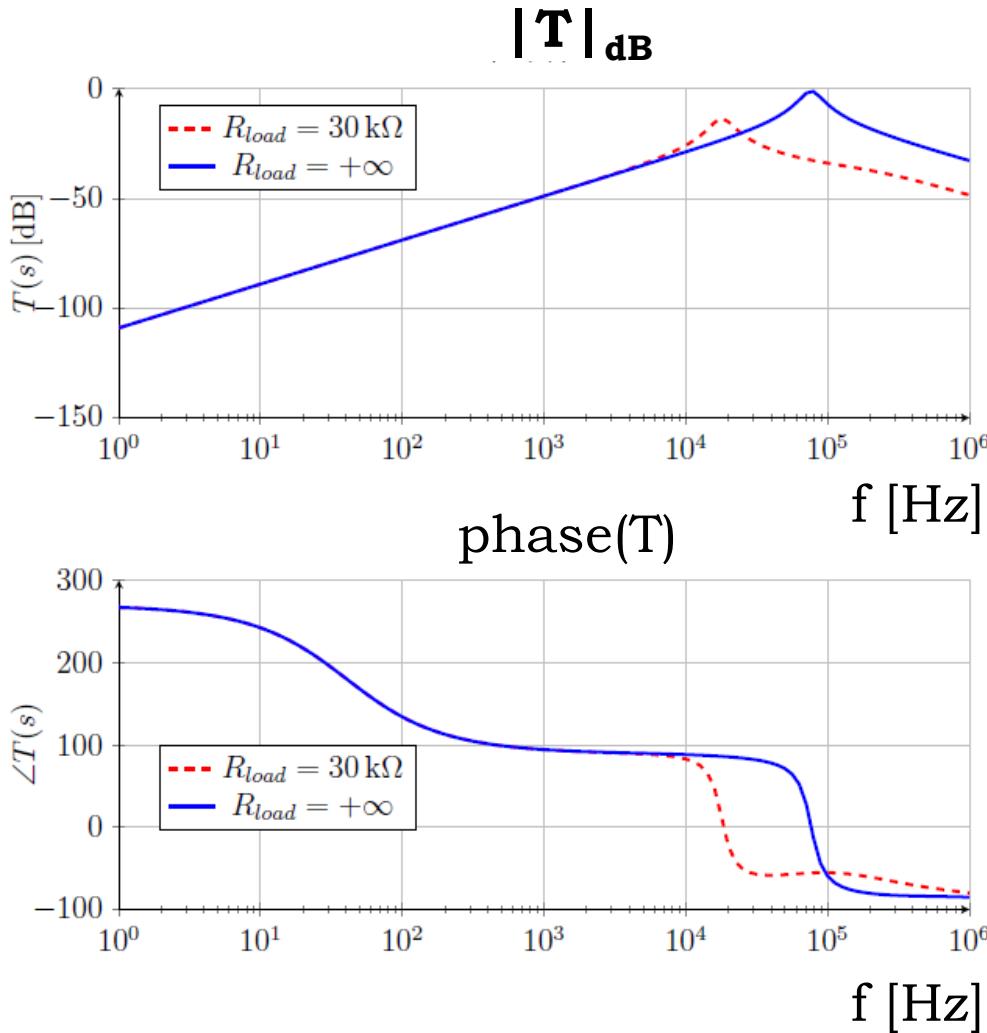


$$R_{in} = \frac{1}{2 \cdot C_2 \cdot f \cdot \sin^2(\Delta\theta)}$$

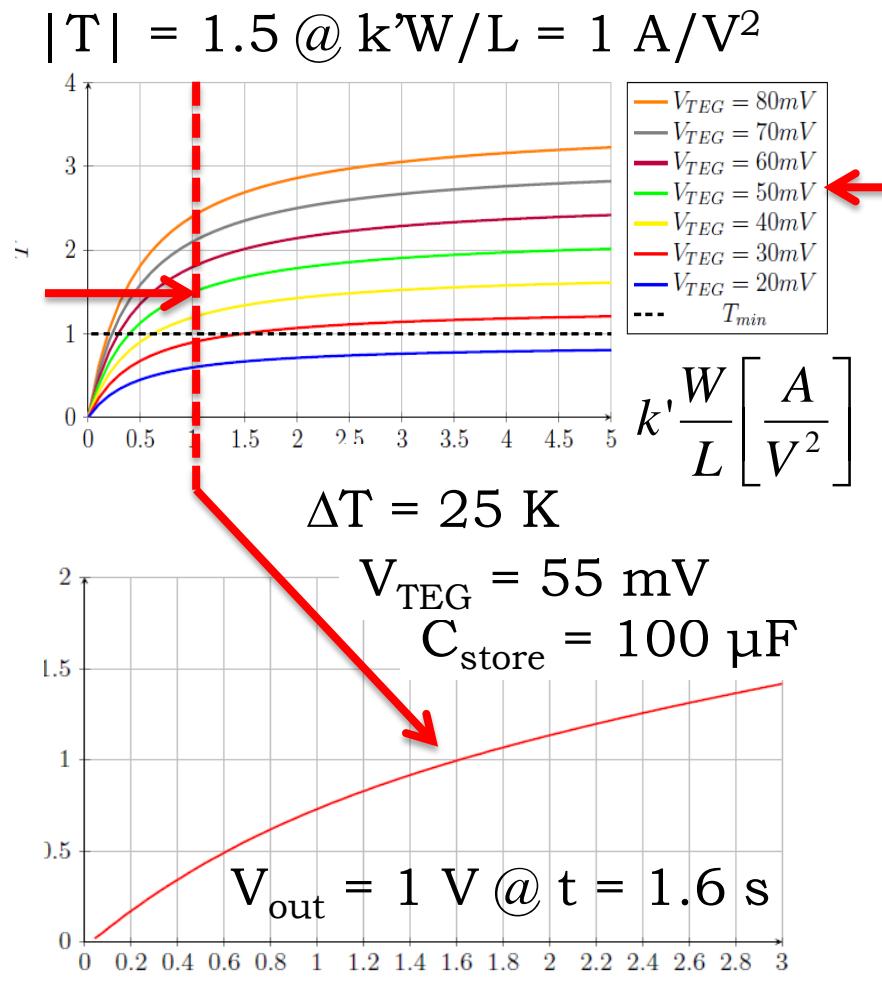
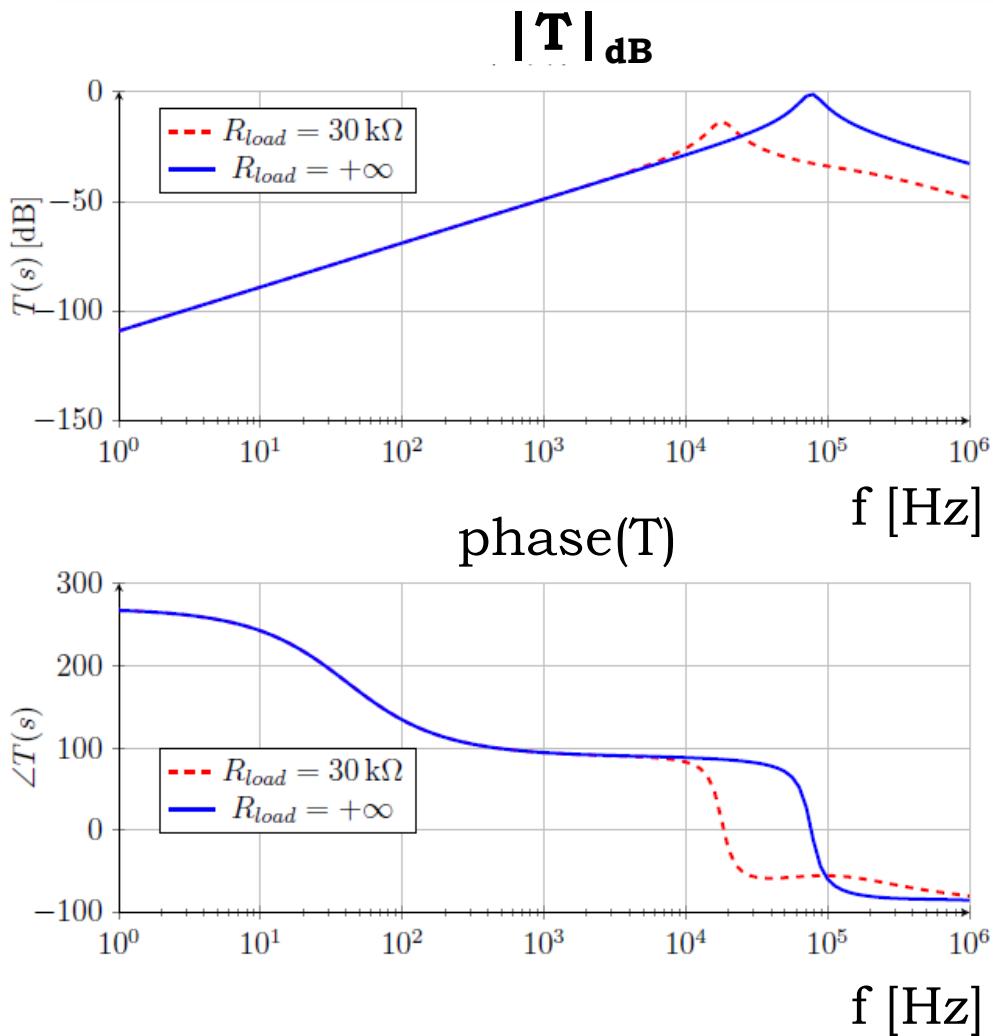
$$\Delta\theta = \frac{\pi}{2} - \arcsin\left(\frac{V_{out}}{V_M} - 1\right)$$



# Loop Gain and Design Curves



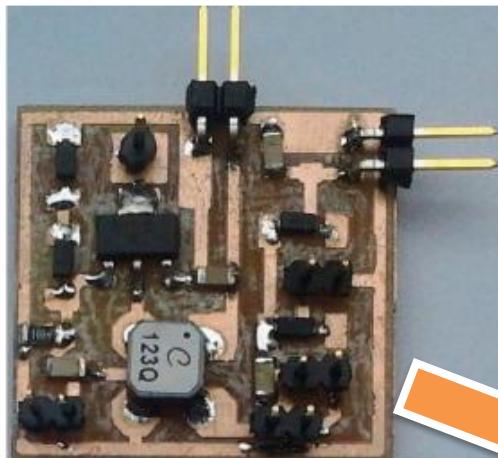
# Loop Gain and Design Curves



# Prototype Supplied with the Thermoelectric Generator

$\Delta T = 10 \text{ K}$

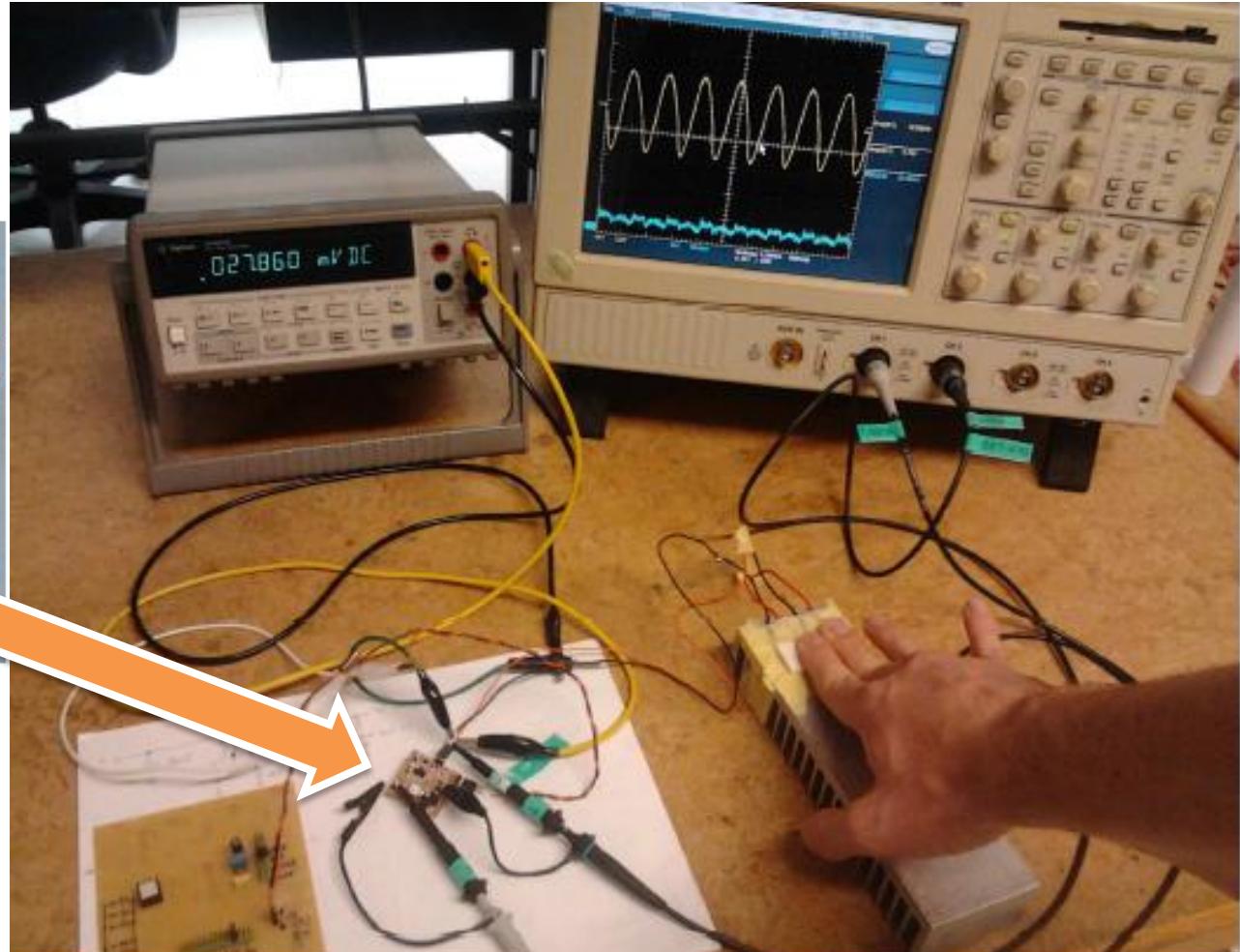
$V_{\text{START-UP}} = 35 \text{ mV}$



$V_{\text{OUT}} = 2.4 \text{ V}$

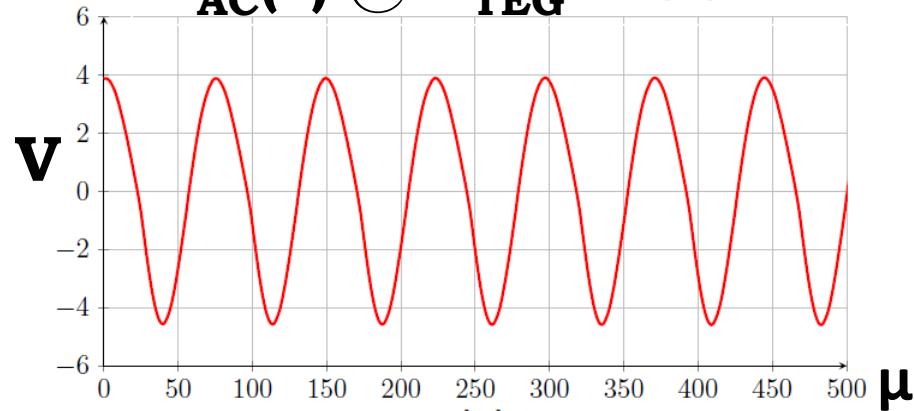
$P_{\text{OUT}} = 60 \mu\text{W}$

$\eta = 25\%$

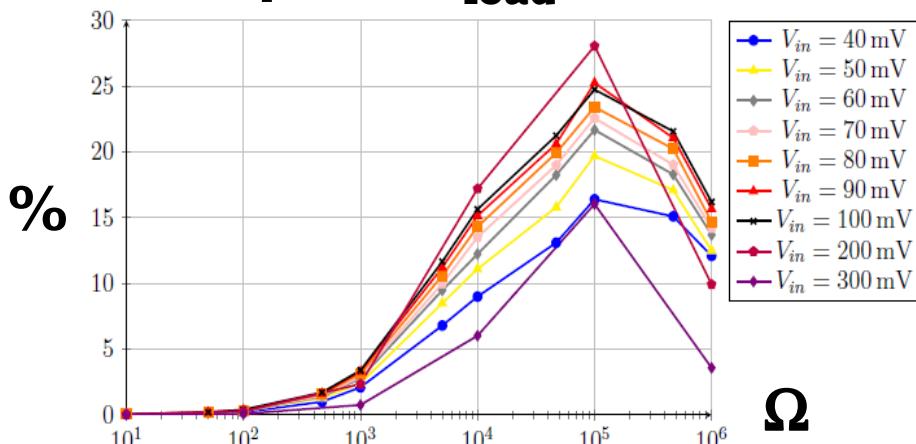


# Test and Measures

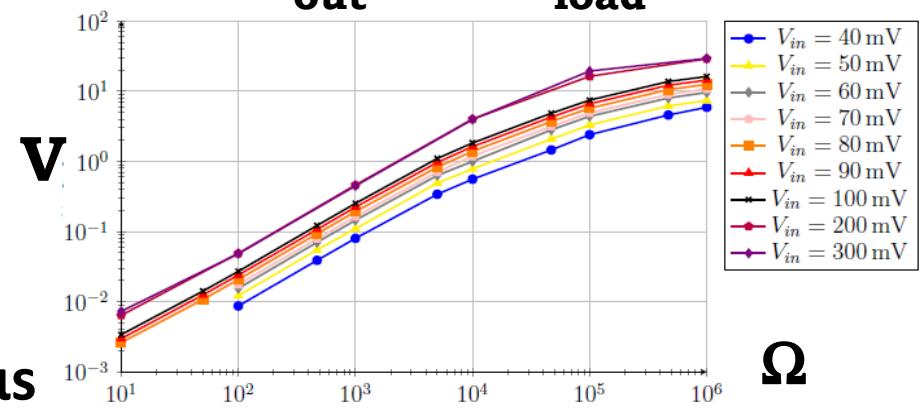
**$V_{AC}(t)$  @  $V_{TEG} = 55$  mV**



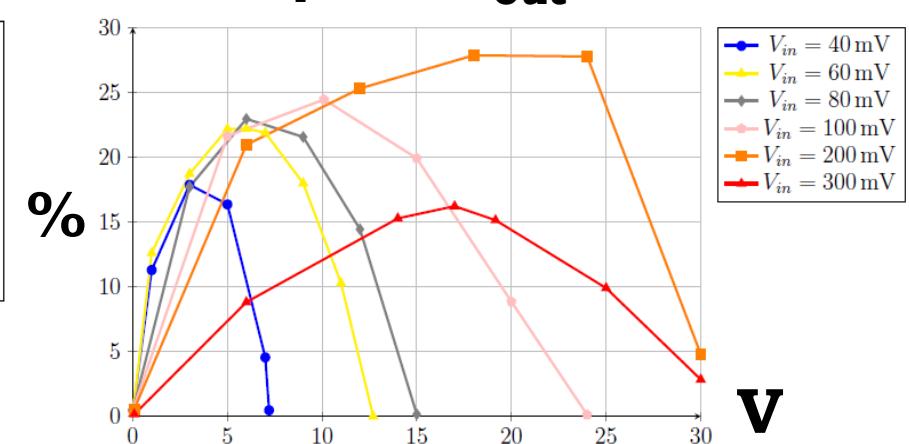
**$\eta$  vs.  $R_{load}$**



**$V_{out}$  vs.  $R_{load}$**



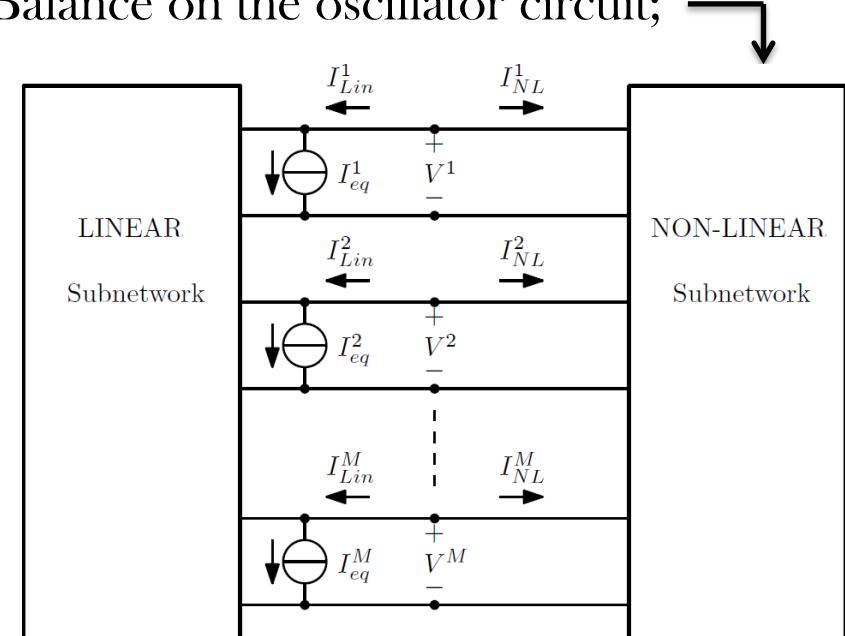
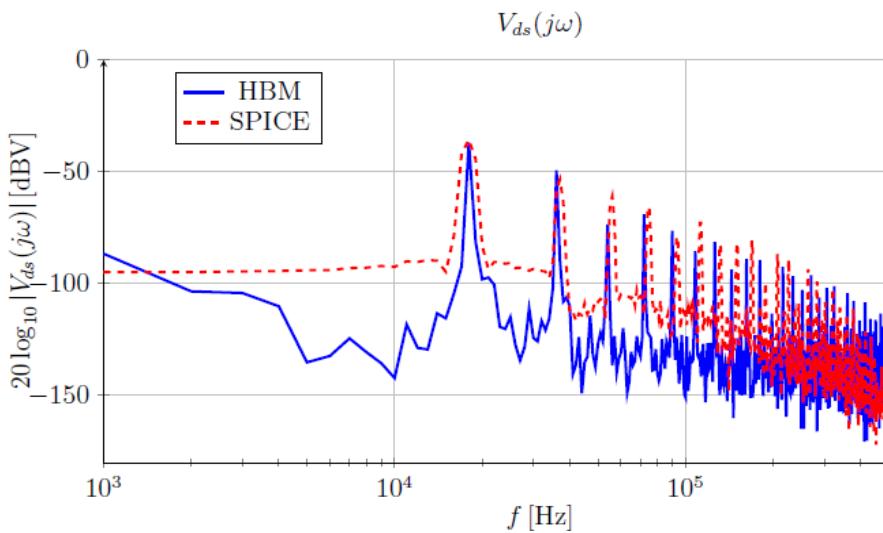
**$\eta$  vs.  $V_{out}$**



# Additional Contribution: Non-Linear Circuit Simulation

Harmonic Balance Method → Piecewise Harmonic Balance

- Preliminary study of the method;
- Application of the Piecewise Harmonic Balance on the oscillator circuit;
- Matlab implementation of the algorithm;
- Simulation and comparison with SPICE.



$$\mathbf{F}(\mathbf{V}) = \mathbf{I}_{\text{Lin}} + \mathbf{I}_{\text{NL}} = 0$$

# Summary

- This thesis focused on a cold-start oscillator for ultra low-voltage sources employed in energy harvesting applications;
- The oscillator and voltage multiplier stages were studied both theoretically and on simulation;
- A prototype of the circuit was developed and tested, the measured start-up voltage is  $V_{\text{start-up}} = 35 \text{ mV}$ ;
- An additional contribution of non-linear circuits simulation: preliminary implementation of the Harmonic Balance Method.